

Exam

Exercise 1: (7 pts)

Consider the circuit shown in figure 1 : $R_1 = R_2 = 6\ \Omega$, $R_3 = 4\ \Omega$, $R_4 = 1\ \Omega$, $E = 12V$, $I = 2A$.

- Using the superposition theorem, Determine the current I_4 flowing in the resistance R_4 .

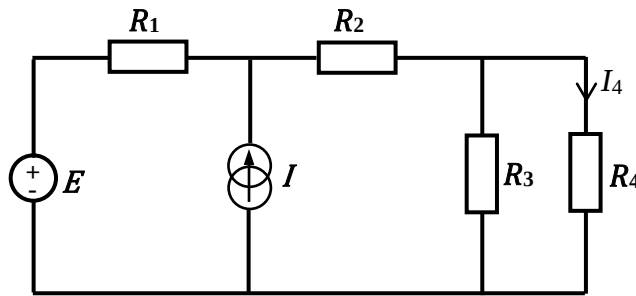


Figure 1

Exercise 2: (6 pts)

Determine the **z-parameters** for the circuit in Figure 2, with: $R = 1\ \Omega$, $C = 1F$, $L = 1H$, $f = 50\ Hz$.

f is the frequency.

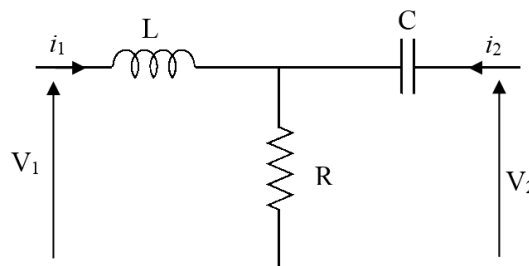


Figure 2

Exercise 3: (7 pts)

Consider the diode circuit shown in Figure 3, D is a silicon diode whose characteristic is linear with $V_0 = 0.7V$ and $r_d = 5\ \Omega$.

The input voltage is in the form: $V_e(t) = 12\sin(\omega t)$, $R_s = 10\ \Omega$.

- 1- Give the equivalent electrical diagram of this diode in the forward and reverse directions.
- 2- Determine the expressions of $i(t)$, $V_D(t)$, and $V_s(t)$.
- 3- Plot $i(t)$, $V_D(t)$, and $V_s(t)$ on the same graph.

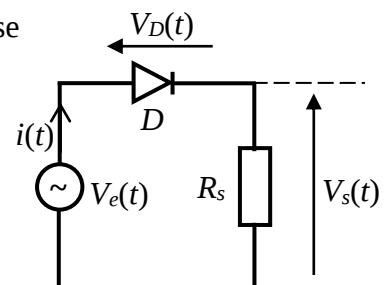
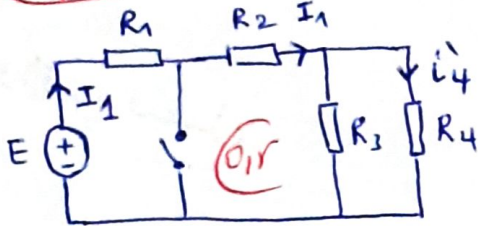


Figure 3

Exercise 1: 7pts

* $I = 0$



$$I_4' = \frac{R_3}{R_3 + R_4} I_1$$

$$I_1 = \frac{E}{R_{eq1}} ; R_{eq1} = (R_1 + R_2) + (R_3 || R_4)$$

$$R_{eq1} = (6 + 6) + \left(\frac{4 \cdot 1}{4 + 1} \right) ; R_{eq1} = 12,8 \Omega$$

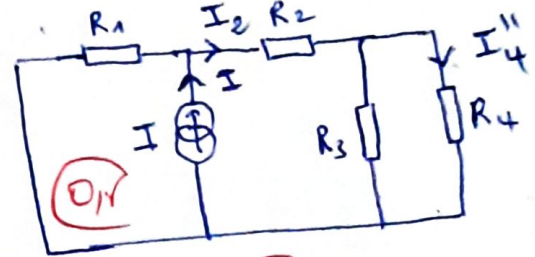
$$I_1 = \frac{E}{R_{eq1}} = \frac{124}{12,8} ; I_1 = 0,93 A$$

$$I_4' = \frac{R_3}{R_3 + R_4} I_1 = \frac{4}{4 + 1} \cdot 0,93$$

$$I_4' = 0,75 A$$

$$I_4 = I_4' + I_4'' = 0,75 + 0,75 = 1,5 A$$

* $E = 0$



$$I_4'' = \frac{R_3}{R_3 + R_4} \cdot I_2$$

$$I_2 = \frac{R_1}{R_1 + R_{eq2}} I ; R_{eq2} = R_2 + (R_3 || R_4)$$

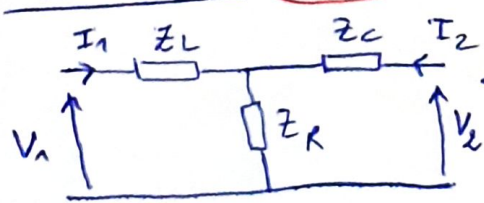
$$R_{eq2} = 6 + \left(\frac{4 \cdot 1}{4 + 1} \right) ; R_{eq2} = 6,8 \Omega$$

$$I_2 = \frac{R_1}{R_1 + R_{eq2}} I = \frac{6}{6 + 6,8} \cdot 2 ; I_2 = 0,93 A$$

$$I_4'' = \frac{R_3}{R_3 + R_4} I_2 = \frac{4}{4 + 1} \cdot 0,93$$

$$I_4'' = 0,75 A$$

Exercise 2: 6pts



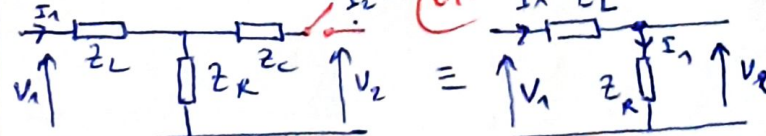
With: $Z_L = jL\omega$, $Z_C = \frac{1}{jC\omega}$, $Z_R = R$

$$\omega = 2\pi f ; f = 50 Hz$$

$$\begin{bmatrix} V_1 \\ V_2 \end{bmatrix} = [Z] \begin{bmatrix} I_1 \\ I_2 \end{bmatrix} = \begin{bmatrix} z_{11} & z_{12} \\ z_{21} & z_{22} \end{bmatrix} \begin{bmatrix} I_1 \\ I_2 \end{bmatrix}$$

$$\begin{cases} V_1 = z_{11} I_1 + z_{12} I_2 \\ V_2 = z_{21} I_1 + z_{22} I_2 \end{cases}$$

1) $I_2 = 0$



$$z_{11} = \frac{V_1}{I_1} ; V_1 = (Z_L + Z_R) I_1$$

$$z_{11} = Z_L + Z_R = jL\omega + R = (1 + j1000)\Omega$$

$$z_{21} = \frac{V_2}{I_1} ; V_2 = Z_R I_1$$

$$z_{21} = Z_R = R = 1 \Omega$$

2) $I_1 = 0$



$$V_1 = Z_{12} I_2 ; V_1 = Z_R I_2 \Rightarrow Z_{12} = Z_R = R = 1 \Omega$$

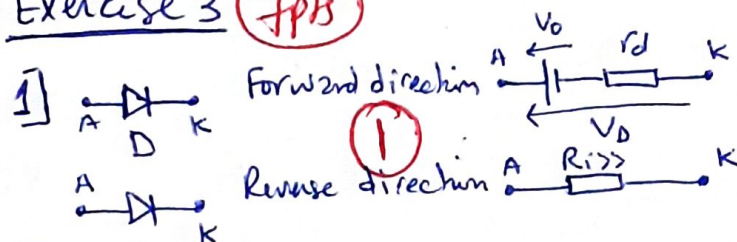
$$V_2 = Z_{22} I_2 \Rightarrow V_2 = (Z_C + Z_R) I_2 \Rightarrow Z_{22} = Z_C + Z_R = \frac{1}{j\omega} + R$$

$$Z_{22} = \left(1 + j \frac{1}{100\pi}\right) \Omega$$

$$[Z] = \begin{bmatrix} Z_{11} & Z_{12} \\ Z_{21} & Z_{22} \end{bmatrix} = \begin{bmatrix} 1 + j100\pi & 1 \\ 1 & 1 - j \frac{1}{100\pi} \end{bmatrix}$$

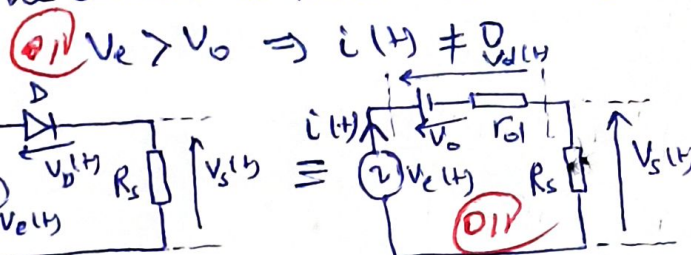
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Exercise 3



2] The diode D is reverse-biased if $V_e \leq V_0 \Rightarrow i(t) = 0$

The diode D is forward-biased if $V_e > V_0 \Rightarrow i(t) \neq 0$



Applying the Voltage Kirchhoff's Law (VKL)

$$V_e(t) = V_0 + (R_d + R_s) i(t)$$

$$i(t) = \frac{V_e(t) - V_0}{R_d + R_s}$$

$$V_d(t) = V_0 + R_d i(t)$$

$$V_d(t) = V_e(t) - R_s i(t)$$

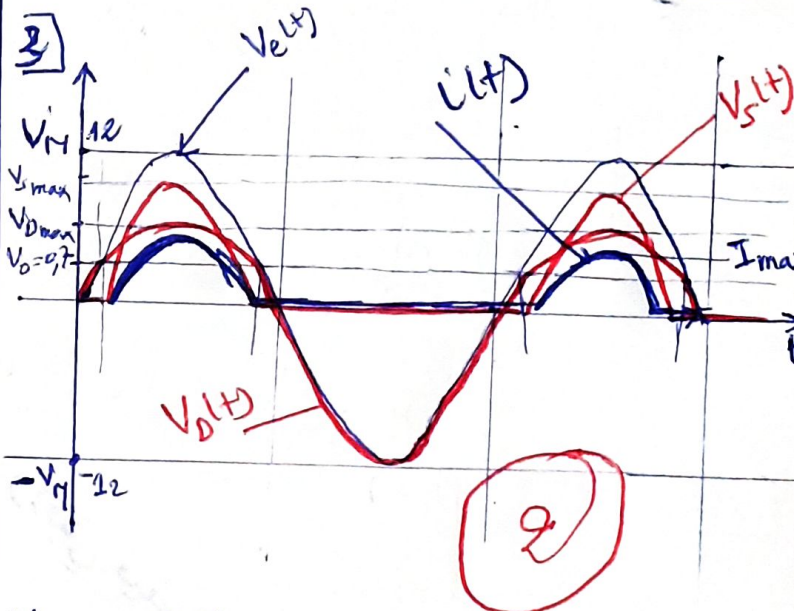
$$V_s(t) = V_e(t) - V_d(t) \Rightarrow V_s(t) = R_s i(t)$$

$$\textcircled{1} \text{ in } \textcircled{2} \Rightarrow V_s(t) = R_s i(t)$$

$$V_d(t) = \begin{cases} V_e(t) & \text{if } i(t) = 0 ; \text{ D is reverse-biased} \\ \frac{R_d}{R_d + R_s} V_e(t) + \frac{R_s}{R_d + R_s} V_0 & \text{if } i(t) \neq 0 ; \text{ D is forward-biased} \end{cases}$$

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$$V_s(t) = \begin{cases} 0 & \text{if } i(t) = 0 ; \text{ D is reverse-biased} \\ R_s \frac{V_e(t) - V_0}{R_s + R_d} & \text{if } i(t) \neq 0 ; \text{ D is forward-biased} \end{cases}$$



$$V_m = 12V$$

$$I_{max} = \frac{V_m - V_0}{R_s + R_d} = 0.75A$$

$$V_{smax} = R_s \frac{V_m - V_0}{R_s + R_d} = 7.1A$$

$$V_{dmax} = \frac{R_d}{R_d + R_s} V_m + \frac{R_s}{R_d + R_s} V_0$$

$$V_{dmax} = 4.46V$$