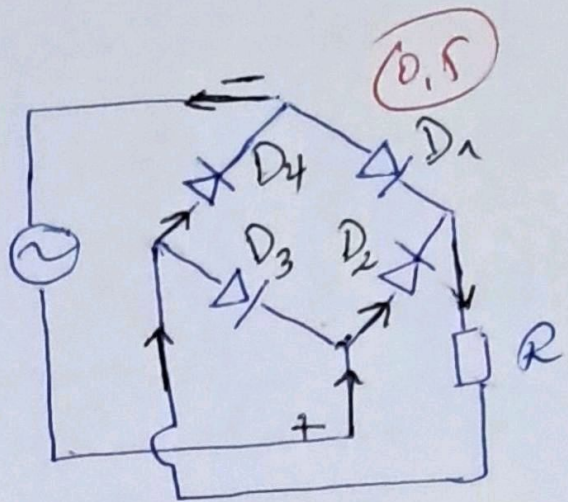
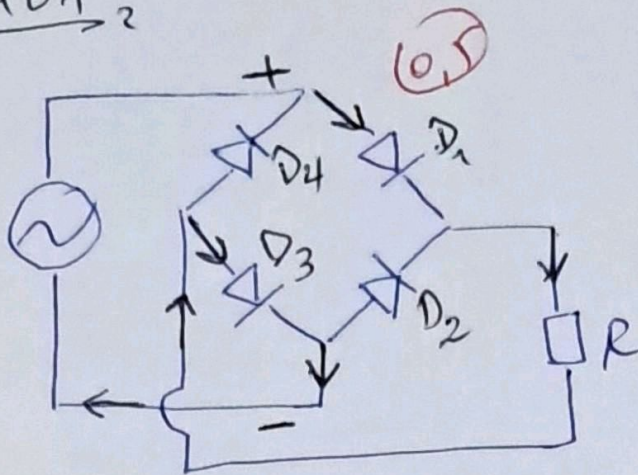
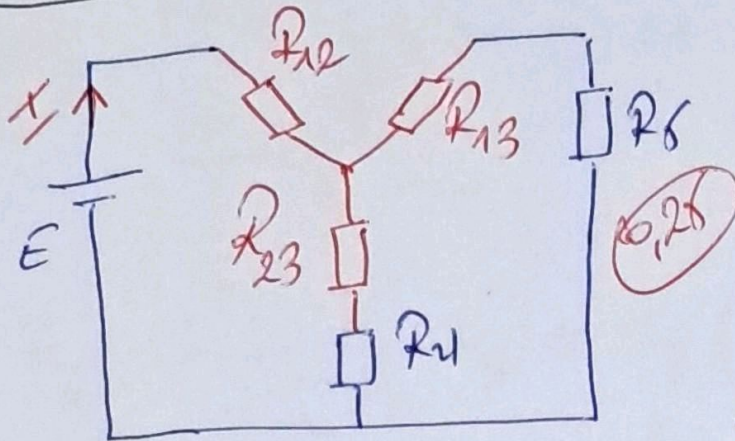


2nd EXAM Solution

EX01



EX02



$$R_{12} = \frac{R_1 R_2}{R_1 + R_2 + R_3} = 30 \Omega \quad (0,25)$$

$$R_{13} = \frac{R_1 R_3}{R_1 + R_2 + R_3} = 30 \Omega \quad (0,25)$$

$$R_{23} = \frac{R_2 R_3}{R_1 + R_2 + R_3} = 30 \Omega \quad (0,25)$$

$$R_{12345} = \frac{(R_{23} + R_4)(R_{13} + R_5)}{(R_{23} + R_4) + (R_{13} + R_5)} = 60 \Omega \quad (0,25)$$

$$R_{eq} = R_{12} + R_{12345} = 30 + 60 = 90 \Omega \quad (0,25)$$

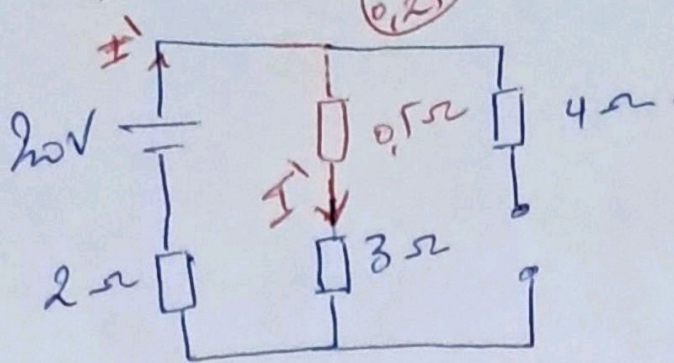
$$I = \frac{E}{R_{eq}} = \frac{45}{90} = 0,5 A$$

$$I = 0,5 A \quad (0,25)$$

$$I_{234} = I_{135} = \frac{I}{2} = 0,25 A \quad (0,25)$$

(01)

Ex03, 2



$$R_{eq} = 0.5 + 3 + 2 = 5.5 \Omega$$

$$(R = \frac{1.1}{1+1} = 0.5 \Omega)$$

$$I' = \frac{E}{R_{eq}} = \frac{20}{5.5} = 3.636 A$$

$$V_3' = R_3 I' = 3 \cdot 3.636$$

$$V_3' = 10.908 V$$

$$(R' = 0.5 + 3 = 3.5 \Omega)$$

$$I' = I_3 + I_2$$

$$I_3 = I' - I_2$$

$$+ R' I_3 - R_2 I_2 = 0$$

$$I_2 = \frac{R'}{R_2} I_3$$

$$I_3 = I' - \frac{R'}{R_2} I_3 \Rightarrow I_3 \left(1 + \frac{R'}{R_2}\right) = I'$$

$$I_3 = \frac{I'}{1 + \frac{R'}{R_2}} = \frac{2}{1 + \frac{3.5}{2}} = 0.727 A$$

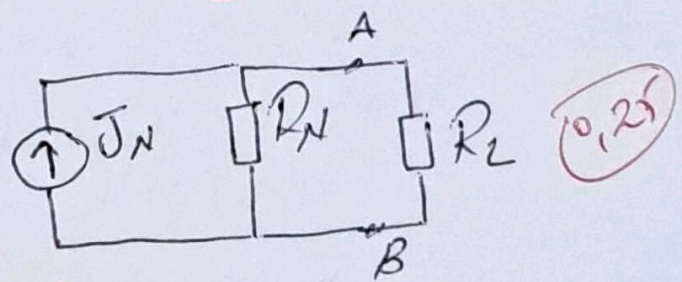
$$V_3'' = R_3 I_3 = 3 \cdot 0.727 = 2.18 V$$

$$V_3 = 2.18 V$$

$$V_3 = V_3' - V_3'' = 8.727 V$$

Ex04 2

$$R_N = R_{th} = (R_4 R_5) // R_6$$

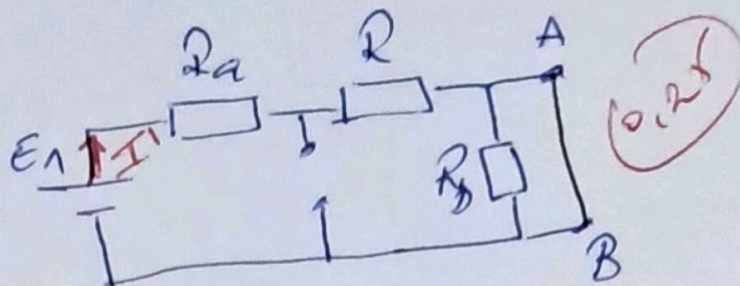


(02)

$$R_N = \frac{(5+3) \cdot 3}{5+3+3} = 2,18 \Omega \quad (0,25)$$

$$E_1 = 100 \text{ V}$$

$$I' = \frac{E_1}{R_{eq}} = \frac{E_1}{R_a + R} \quad (0,25)$$



$$I' = \frac{100}{5+3} = 12,5 \text{ A} \quad (0,5)$$

$$J = 7 \text{ A}$$

$$J = I_{Ra} + I_R$$

$$= \frac{V}{R_a} + \frac{V}{R} \Rightarrow V = \frac{R_a R}{R_a + R} J \quad (0,25)$$

$$V = \frac{5 \cdot 3}{5+3} \cdot 7 = 13,125 \text{ V} \quad (0,25)$$

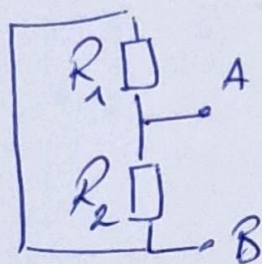
$$I_R = \frac{V}{R} = \frac{13,125}{3} = 4,375 \text{ A} \quad (0,25)$$

$$I_N = I' + I_R = 12,5 + 4,375 \Rightarrow I_N = 16,875 \text{ A} \quad (0,5)$$

EX052

$$R_H = R_1 \parallel R_2$$

$$R_H = \frac{R_1 R_2}{R_1 + R_2} \quad (0,25)$$



$$R_H = \frac{6 \cdot 10^3 \cdot 3 \cdot 10^3}{(6+3) \cdot 10^3}$$

$$R_H = 2 \text{ K} \Omega \quad (0,25)$$

$$E_H = E - R_1 I - R_2 I = 0 \Rightarrow I = \frac{E}{R_1 + R_2} = \frac{12}{9 \cdot 10^3}$$

$$I = 1,33 \cdot 10^{-3} \text{ A} \quad (0,25)$$

(03)

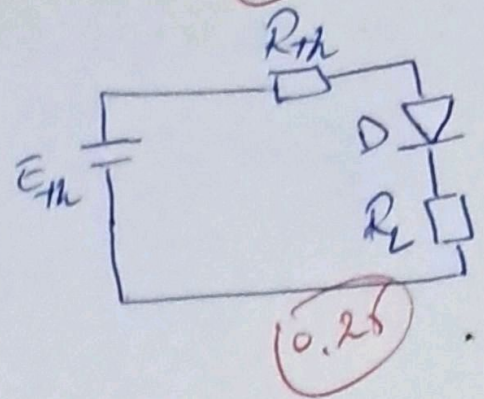
$$E_H = R_2 I = \frac{R_2}{R_1 + R_2} E \Rightarrow E_H = 4V \quad (0,25)$$

Ideal diode

$$E_H - R_H I_I - R_L I_I = 0 \quad (0,25)$$

$$I_I = \frac{E_H}{R_H + R_L} = \frac{4}{(2+1)10^3}$$

$$I_I = 1,33 \cdot 10^{-3} A \quad (0,5)$$



Perfect diode

$$E_H - R_H I_P - V_H - R_L I_P = 0 \Rightarrow I_P = \frac{E_H - V_H}{R_H + R_L} \quad (0,25)$$

$$I_P = 1,13 \cdot 10^{-3} A \quad (0,5)$$

EX062

$$I = I_S \left(e^{\frac{V_d}{V_T}} - 1 \right), I \approx I_S e^{\frac{V_d}{V_T}} \quad (0,5)$$

$$V_d = V_T \ln \left(\frac{I}{I_S} \right) \quad (0,5)$$

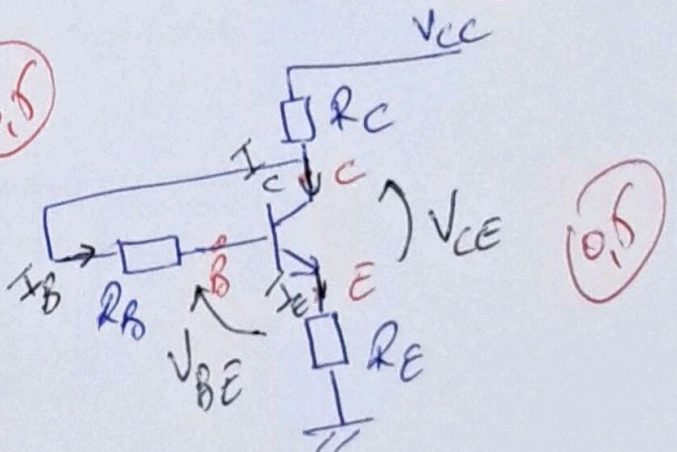
$$V_T = \frac{KT}{e} = \frac{1,38 \cdot 10^{-23} \cdot 300}{1,6 \cdot 10^{-19}} = 0,025 V \quad (0,5)$$

$$V_d = 0,025 \ln \left(\frac{2 \cdot 10^{-3}}{2 \cdot 10^{-9}} \right) = 0,36 V \quad (0,5)$$

EX072

$$I_C = \beta I_B \Rightarrow I_B = \frac{I_C}{\beta} \quad (0,5)$$

$$I_E = I_C + I_B = I_C \left(1 + \frac{1}{\beta} \right) \quad (0,5)$$



(04)

$$1) V_{CC} - R_C(I_C + I_B) - V_{CE} - R_E I_E = 0 \quad (0.5)$$

$$V_{CC} - V_{CE} = R_C \left(I_C + \frac{I_C}{\beta} \right) + R_E \left(I_C + \frac{I_C}{\beta} \right)$$

$$V_{CC} - V_{CE} = I_C \left(R_C \left(1 + \frac{1}{\beta} \right) + R_E \left(1 + \frac{1}{\beta} \right) \right)$$

$$I_C = \frac{V_{CC} - V_{CE}}{R_C \left(1 + \frac{1}{\beta} \right) + R_E \left(1 + \frac{1}{\beta} \right)} \quad (0.5)$$

$$\beta \gg 1 \Rightarrow I_C = \frac{V_{CC} - V_{CE}}{R_C + R_E} \quad (0.25)$$

The circuit is stable.

$$2) V_{CC} - R_C(I_C + I_B) - R_B I_B - V_{BE} - R_E I_E = 0 \quad (0.5)$$

$$V_{CC} - V_{BE} = R_C I_C \left(1 + \frac{1}{\beta} \right) + R_B \frac{1}{\beta} I_C + R_E I_C \left(1 + \frac{1}{\beta} \right)$$

$$V_{CC} - V_{BE} = I_C \left(R_C \left(1 + \frac{1}{\beta} \right) + R_B \frac{1}{\beta} + R_E \left(1 + \frac{1}{\beta} \right) \right)$$

$$I_C = \frac{V_{CC} - V_{BE}}{R_C \left(1 + \frac{1}{\beta} \right) + R_B \frac{1}{\beta} + R_E \left(1 + \frac{1}{\beta} \right)} \quad (0.5)$$

$$\beta \gg 1 \Rightarrow I_C = \frac{V_{CC} - V_{BE}}{R_C + \frac{R_B}{\beta} + R_E} \quad (0.25)$$

The circuit is not stable.

(0.5)