

### Exercise 01: QCM

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| <p>1. Which of the following best describes the CIA triad?</p> <ol style="list-style-type: none"> <li>Confidentiality, Integrity, Availability</li> <li>Control, Isolation, Authentication</li> <li>Confidentiality, Identification, Authorization</li> <li>Consistency, Integrity, Accountability</li> </ol> <p>2. Authentication is the process of :</p> <ol style="list-style-type: none"> <li>Determining the actions of the user</li> <li>Verifying the identity of a user</li> <li>Encrypting data before transmission</li> <li>Monitoring system activity</li> </ol> <p>3. Which of the following attacks target availability?</p> <ol style="list-style-type: none"> <li>Identity theft</li> <li>Denial of service</li> <li>Journal modification</li> <li>Bombardment and saturation of the network</li> </ol> <p>4. Which statement is correct?</p> <ol style="list-style-type: none"> <li>Security failures are always accidental</li> <li>Safety considers malicious behavior</li> <li>Security focuses on intentional attacks</li> <li>Safety and security are identical concepts</li> </ol> <p>5. Which statement is correct?:</p> <ol style="list-style-type: none"> <li>A threat is the same as a risk</li> <li>Risk exists only if an attack has occurred</li> <li>A threat exploits a vulnerability to create risk</li> <li>Risk depends only on system vulnerabilities</li> </ol> <p>6. The primary goal of physical security is to:</p> <ol style="list-style-type: none"> <li>Protect data confidentiality</li> <li>Prevent unauthorized physical access and damage</li> <li>Detect malware infections</li> <li>Ensure software correctness</li> </ol> | <p>7. Information integrity means that data:</p> <ol style="list-style-type: none"> <li>Is encrypted</li> <li>Is always available</li> <li>Has not been altered without authorization</li> <li>Is stored securely</li> </ol> <p>8. Which of the following best defines an active attack?</p> <ol style="list-style-type: none"> <li>Monitoring network traffic</li> <li>Reading sensitive files</li> <li>Altering data or system behavior</li> <li>Collecting metadata</li> </ol> <p>9. Which is an example of an operational security control?</p> <ol style="list-style-type: none"> <li>Firewalls</li> <li>Encryption algorithms</li> <li>Change management procedures</li> <li>Secure boot</li> </ol> <p>10. Which is an example of a passive attack?</p> <ol style="list-style-type: none"> <li>A. Denial-of-service attack</li> <li>Man-in-the-middle altering messages</li> <li>Eavesdropping on network traffic</li> <li>SQL injection</li> </ol> <p>11. Which of the following is an example of a logical security failure?</p> <ol style="list-style-type: none"> <li>Server room fire</li> <li>Hard disk theft</li> <li>Weak password policy</li> <li>Power outage</li> </ol> <p>12. Which dimension is not part of the IT security architecture?</p> <ol style="list-style-type: none"> <li>Technical dimension</li> <li>Monetary dimension</li> <li>Organizational dimension</li> <li>Legal dimension</li> </ol> |
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### Exercise 02:

- Explain the difference between identification and authentication.
- What is the relationship between: authentication, integrity, and non-repudiation.
- Give examples of attackers in the real world.
- Why are hackers interested in corporate information systems?
- What is the difference between computer security and cybersecurity?

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## Correction

### Exercise 1:

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| <p>13. Which of the following best describes the CIA triad?</p> <ul style="list-style-type: none"><li>a. Confidentiality, Integrity, Availability</li><li>b. Control, Isolation, Authentication</li><li>c. Confidentiality, Identification, Authorization</li><li>d. Consistency, Integrity, Accountability</li></ul> <p>14. Authentication is the process of :</p> <ul style="list-style-type: none"><li>a. Determining the actions of the user</li><li>b. Verifying the identity of a user</li><li>c. Encrypting data before transmission</li><li>d. Monitoring system activity</li></ul> <p>15. Which of the following attacks target availability?</p> <ul style="list-style-type: none"><li>a. Identity theft</li><li>b. Denial of service</li><li>c. Journal modification</li><li>d. Bombardment and saturation of the network</li></ul> <p>16. Which statement is correct?</p> <ul style="list-style-type: none"><li>a. Security failures are always accidental</li><li>b. Safety considers malicious behavior</li><li>c. Security focuses on intentional attacks</li><li>d. Safety and security are identical concepts</li></ul> <p>17. Which statement is correct?</p> <ul style="list-style-type: none"><li>a. A threat is the same as a risk</li><li>b. Risk exists only if an attack has occurred</li><li>c. A threat exploits a vulnerability to create risk</li><li>d. Risk depends only on system vulnerabilities</li></ul> <p>18. The primary goal of physical security is to:</p> <ul style="list-style-type: none"><li>a. Protect data confidentiality</li><li>b. Prevent unauthorized physical access and damage</li><li>c. Detect malware infections</li><li>d. Ensure software correctness</li></ul> | <p>19. Information integrity means that data:</p> <ul style="list-style-type: none"><li>a. Is encrypted</li><li>b. Is always available</li><li>c. Has not been altered without authorization</li><li>d. Is stored securely</li></ul> <p>20. Which of the following best defines an active attack?</p> <ul style="list-style-type: none"><li>a. Monitoring network traffic</li><li>b. Reading sensitive files</li><li>c. Altering data or system behavior</li><li>d. Collecting metadata</li></ul> <p>21. Which is an example of an operational security control?</p> <ul style="list-style-type: none"><li>a. Firewalls</li><li>b. Encryption algorithms</li><li>c. Change management procedures</li><li>d. Secure boot</li></ul> <p>22. Which is an example of a passive attack?</p> <ul style="list-style-type: none"><li>a. A. Denial-of-service attack</li><li>b. Man-in-the-middle altering messages</li><li>c. Eavesdropping on network traffic</li><li>d. SQL injection</li></ul> <p>23. Which of the following is an example of a logical security failure?</p> <ul style="list-style-type: none"><li>a. Server room fire</li><li>b. Hard disk theft</li><li>c. Weak password policy</li><li>d. Power outage</li></ul> <p>24. Which dimension is not part of the IT security architecture?</p> <ul style="list-style-type: none"><li>e. Technical dimension</li><li>f. Monetary dimension</li><li>g. Organizational dimension</li><li>h. Legal dimension</li></ul> |
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### Exercise 2:

**1. Explain the difference between identification and authentication.**

Identification = knowing the identity of an entity (who I am).

Authentication = proving the identity of an entity

**2. What is the relationship between: authentication, integrity, and non-repudiation?**

The relationship is one of inclusion: integrity  $\subset$  authentication  $\subset$  non-repudiation.

**3. Give examples of attackers in the real world.**

- A government
- A criminal or a terrorist
- Industrial or commercial spy (competitor) **Howawi Samsung**
- Internal employee

**4. Why are hackers interested in corporate information systems?**

- Financial gains: access to information, then monetization and resale (customer files, user files, emails, passwords, etc.)
- Resource usage: bandwidth and storage space, Zombies (botnets).
- Blackmail: preventing access to resources
- Gathering information on the system: industrial/competitive, state espionage.

**5. What is the difference between computer security and cybersecurity?**

- Computer security concerns all computer systems, whether or not they are connected to the internet or networks.
- Cybersecurity concerns computer systems connected to the internet or networks.

## TD N°02

### *Classical Cryptography*

#### Exercise No. 01:

- Find the coefficients  $u$ ,  $v$  and the GCD of the following integers:

- $(a, b) = (60, 19)$

$$60 = 19 * 3 + 3 \rightarrow 3 = 60 - 19 * 3$$

$$19 = 3 * 6 + 1 \rightarrow 1 = 19 - 3 * 6 = 19 - (60 - 19 * 3) * 6$$

$$1 = 19 * 19 - 60 * 6$$

$$u=-6, v=19, \text{GCD}=1$$

- $(a, b) = (280, 11)$

$$u=-2, v=51, \text{GCD}=1$$

- $(a, b) = (38, 26)$

$$u=-2, v=3, \text{GCD}=2$$

- Calculate the inverse of:

- $41^{-1} \bmod 53$ .

To calculate the modular inverse of  $41 \bmod 53$ , we use the extended Ecluse algorithm to find the  $\text{GCD}(53,41)$  and the coefficient  $v$ . The condition is  $\text{GCD}=1$

$$\underbrace{(53)}_A \times \underbrace{-17}_u + \underbrace{(41)}_B \times \underbrace{22}_v = \underbrace{1}_{\text{PGCD}(A,B)}$$

$$v=22, \text{ then } 41^{-1} \bmod 53 = 22$$

- $317^{-1} \bmod 521$

$$\underbrace{(521)}_A \times \underbrace{-101}_u + \underbrace{(317)}_B \times \underbrace{166}_v = \underbrace{1}_{\text{PGCD}(A,B)}$$

$$v=166, \text{ then } 317^{-1} \bmod 521=166$$

- $24^{-1} \bmod 512$

$$\underbrace{(512)}_A \times \underbrace{1}_u + \underbrace{(24)}_B \times \underbrace{-21}_v = \underbrace{8}_{\text{PGCD}(A,B)}$$

$\text{GCD}(512,24)=8 \neq 1$ . Therefore, there is no

## Exercise No. 2: ( Shift cipher )

1. Write a pseudo-code for encrypting/decrypting a text using Caesar.

### Encryption:

```
char indtolettre (int ind)
int j=0;
while j<26
{ if j == ind
return alpha[j] j
else j++
}
```

```
int lettretoind (char lettre)
int j=0;
while j<26
{ if t[j] == letter
return j
else j++
}
```

### %Encryption

```
char p[], c[], k
char alph[] = {'A','B','C', ..., 'Z'} % alphabet array
int l, i, k1
l = length(p);
k1 = lettretoind (k)
for (i:=0; i< l; i=i+1 )
c[i]= indtoletter ( lettretoind (p[i]) + k1 % 26)
```

### % Decryption:

```
l = length(p);
k1 = lettretoind (k)
for (i:=0; i< l; i=i+1 )
p[i]= indtoletter ( lettretoind (p[i]) - k1 + 26 % 26)
```

2. Prove that  $D_k(E_k(m))=m$ .

Let  $c=E_k(m)=m+k \bmod 26$  and  $m=D_k(c)=c-k \bmod 26$

$$\begin{aligned} D_k(E_k(m)) &= D_k(m+k \bmod 26) = (m+k \bmod 26) - k \bmod 26 \\ &= m \end{aligned}$$

3. Encrypt the text "CRYPTOGRAPHY" with the key K.

We apply the encryption function  $E_k(m)=m+k \bmod 26$  where  $k=10$

| Plain text     | C  | R  | Y  | P  | T  | O  |
|----------------|----|----|----|----|----|----|
| Clue. Clear    | 2  | 17 | 24 | 15 | 19 | 14 |
| Key            | K  | K  | K  | K  | K  | K  |
| Clue. Key      | 10 | 10 | 10 | 10 | 10 | 10 |
| Ind. Chiff     | 12 | 1  | 8  | 25 | 3  | 24 |
| Encrypted text | M  | B  | I  | Z  | D  | Y  |

$$E_k(\text{CRYPTOGRAPHY}) = \text{MBIZDYQBKZRSO}$$

4. Decrypt the text "JSHZZPXBL" using the key H.

We apply the decryption function  $D_k(c) = c - k \bmod 26$  where  $k = 7$

(In the table, encrypt only the word "ENCRYPT")

$$D_k(\text{JSHZZPXBL}) = \text{CLASSIC}$$

#### Exercise No. 4: (Vigenère cipher)

1. Write a pseudo-code for encrypting/decrypting a text using Vigenère.

Input: char p[], char k[]

Output: char c[]

$l = \text{length}(k)$

For  $i=0$  to  $\text{length}(p)-1$

$c[i] = \text{indtoletter}(\text{lettertoind}(p[i]) + \text{lettertoind}(k[i \% l]) \% 26)$

2. Encrypt the text "CRYPTOGRAPHY" with the key "SECRET".

The encryption function is applied.  $E_k(x_1, x_2, \dots, x_n) = (x_1 + k_1, x_2 + k_2, \dots, x_n + k_n)$

$$E_k(\text{CRYPTOGRAPHY}) = \text{UVAGXHYVCGLBW}$$

3. Decipher the text "ORABCNDIBDIVD" using the key "KEY":

The decryption function is applied.  $D_k(y_1, y_2, \dots, y_n) = (y_1 - k_1, y_2 - k_2, \dots, y_n - k_n)$

$$D_k(\text{ORABCNDIBDIVD}) = \text{ENCRYPTEDTEXT}$$

#### Exercise No. 5: (Affine Cipher)

Let  $K = (5, 11)$

1. Prove that  $D_k(E_k(m)) = m$

- $E_k(x) = ax + b \bmod 26$
- $D_k(y) = a^{-1} \cdot (y - b) \bmod 26$

$$D_k(y) = a^{-1} \cdot (y - b) \bmod 26 = a^{-1} \cdot (ax + b - b) \bmod 26$$

$$= a^{-1} \cdot ax \bmod 26$$

$$= x$$

2. Calculate the encryption and decryption functions,

Let  $K = (5, 11)$

$$E_k(x) = 5x + 11 \bmod 26$$

We calculate  $5^{-1} \bmod 26$

$$26 = 5 \cdot 5 + 1 \Rightarrow 1 = 26 - 5 \cdot 5$$

$$5^{-1} \bmod 26 = -5 = -5 + 26 = 21$$

$$\text{Then } D_k(y) = 21(y - 11) \bmod 26 = 21y - 21 \cdot 11 \bmod 26 = 21y - 23 \bmod 26 = (21y + 3) \bmod 26$$

3. Encrypt the following word: "AFFINE"

Use a table like in exercise 2 and apply the function  $E_k(x) = 5x + 11 \bmod 26$

The encrypted text is: LKKZYF

|   |   |   |   |   |   |   |   |   |   |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |
|---|---|---|---|---|---|---|---|---|---|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|
| A | B | C | D | E | F | G | H | I | J | K  | L  | M  | N  | O  | P  | Q  | R  | S  | T  | U  | V  | W  | X  | Y  | Z  |
| 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 | 25 |

### Exercise No. 5: ( Transposition Cipher )

The password is "SAMI"

1. Encrypt the text " COMPUTER SCIENCE "
2. Decipher the text "YEMSRQITEXXU"

#### 1. Encryption:

|   |   |   |   |
|---|---|---|---|
| S | A | M | I |
| 4 | 1 | 3 | 2 |
| I | N | F | O |
| R | M | A | T |
| I | Q | U | E |

|   |   |   |   |
|---|---|---|---|
| A | I | M | S |
| 1 | 2 | 3 | 4 |
| N | O | F | I |
| M | T | A | R |
| Q | E | U | I |

Encrypted text: NOFIMTARQEUI

#### 2. Decrpting

|   |   |   |   |
|---|---|---|---|
| A | I | M | S |
| 1 | 2 | 3 | 4 |
| Y | E | M | S |
| R | Q | I | T |
| E | X | X | U |

|   |   |   |   |
|---|---|---|---|
| S | A | M | I |
| 4 | 1 | 3 | 2 |
| S | Y | M | E |
| T | R | I | Q |
| U | E | X | X |

Plain text: Symmetrique

### Exercise 6:

Without knowing the key, decrypt the first 9 letters of the following message using the shift algorithm.

**ATKGIZOUTSGRBKORRGZKWAUIUSVXUSKZRGYKIAOXZKJKYJUTTKKYUAYEYZSKYJOTLUXSGZOWAK**

We use frequency analysis, the most frequent letter in the ciphertext is K(10), and the most frequent letter in the French text is E(4).

$$c = m + K \bmod 26 \rightarrow k = c - m \bmod 26 \rightarrow k = 10 - 4 = 6$$

The decryption function is:  $m = c - 6 \bmod 26$

So, the first 9 letters of the plain text are: **AN ACTION**

### Exercise N° 01: *diagram of Feistel*

1. Write the encryption formulas with the Feistel scheme according to iteration  $i$ ,

$$L_i = R_{i-1},$$

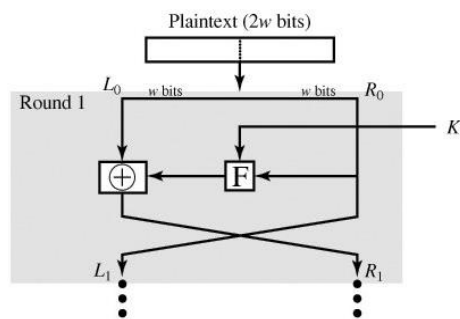
$$R_i = L_{i-1} \oplus F(R_{i-1}, K_i)$$

2. Write the decryption formulas with this scheme according to iteration  $i$ ,

$$R_{i-1} = L_i$$

$$L_{i-1} = R_i \oplus F(R_i, K_i)$$

3. Draw this scheme for encryption



4. Apply this scheme on:
  - The block: 11010110
  - The key ( $K_0$ ): 1010
  - $F(x, k) = x \oplus k$
  - $K_i = K_{i-1} \oplus 1011$
  - Number of iterations: 3.

| $i$   | 1    | 2    | 3    |
|-------|------|------|------|
| $K_i$ | 0001 | 1010 | 0001 |
| $L_i$ | 0110 | 1010 | 1100 |
| $R_i$ | 1010 | 1100 | 0111 |

The encrypted block is: 11010110

### Exercise N° 02: AES

1. Define the four transformations of the AES

**SubByte:** substitution of bytes in the state table

**ShiftRow:** shift of rows in the status table

**MixColumn:** moving columns in the status table (except last round)

**AddRoundKey:** addition of a "round key" that varies with each round.

2. Apply SubBytes to byte (01001001).

0100 1001

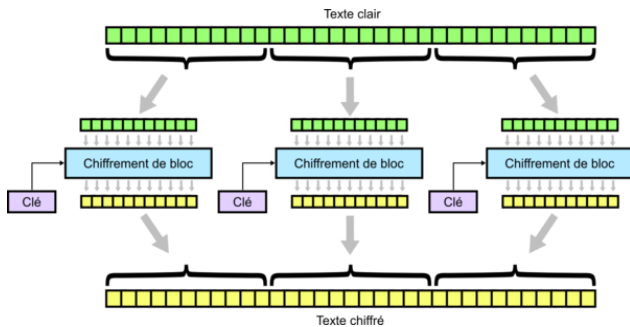
4 9 → we use the S-box matrix to find the value of line 4 and column 9  
The result is **3b**, so the new byte is: **00111011**

3. Apply ShiftRow to the table:

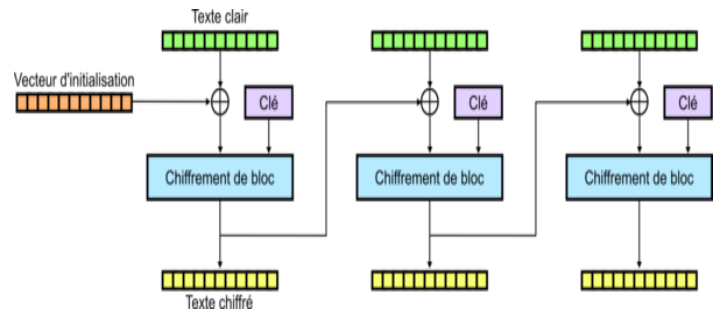
|    |     |    |    |
|----|-----|----|----|
| 34 | 9a  | aa | 01 |
| 00 | 0e  | 67 | f4 |
| fb | 5th | 89 | ff |
| c5 | 00  | e4 | cc |

### Exercise N° 03: Modes of operation

Be the schemas of symmetric encryption operation modes:



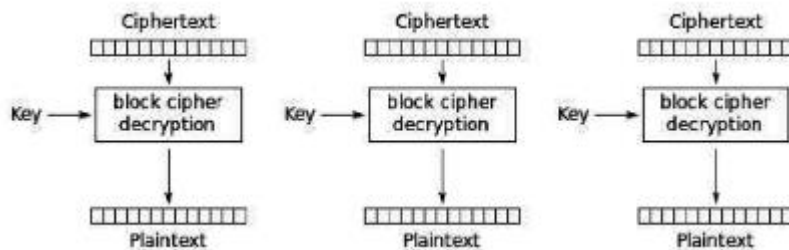
(1) ECB



(2) CBC

1. The ECB mode:

- Draw the decryption diagram.



- Deduce the encryption/decryption functions.

Encryption:  $C_i = E_K(P_i)$

Decryption:  $P_i = D_K(C_i)$

- What is the problem with this mode?

The repetitions of clear message fragments are not masqued and are found in the form of repeated fragments in the encrypted message.

- Calculate the ciphertext:

$M = 101100011011101$

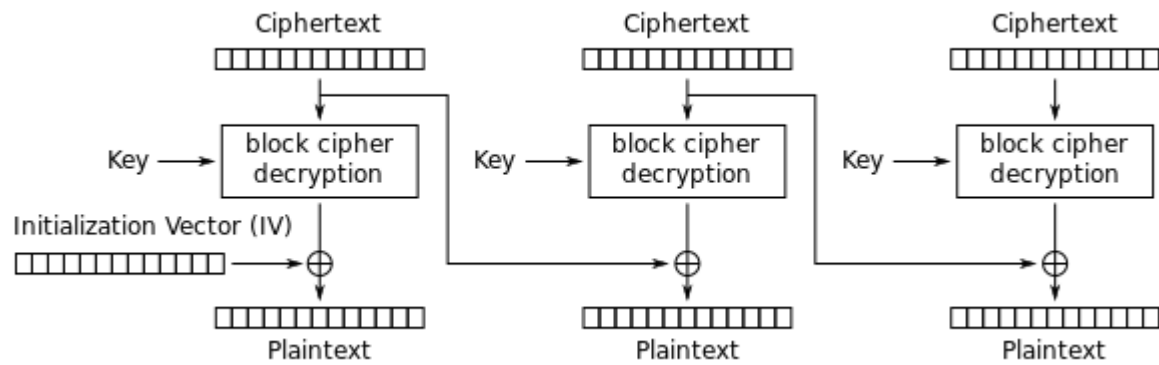
We have a 4-bit size key, so the block size is 4 bits.

$B_1=1011$ ,  $B_2=0001$ ,  $B_3=1011$ ,  $B_4=101\ 0$  (add a bit in the least significant bit (LSB) of value 0)

The cipher text is: 0111001001110101

2. The CBC mode:

- Draw the decryption diagram.



- Deduce the encryption/decryption functions.

Encryption:  $C_i = E_K(P_i \oplus C_{i-1})$

Decryption:  $P_i = D_K(C_i) \oplus C_{i-1}$

- Calculate the ciphertext:

We apply the encryption function after splitting the message into blocks.

0010011010110010

### Exercise No. 01: (Mathematical concepts)

Apply Fermat's test on  $p=11$ , with  $a=2$  and  $a=3$ .

- $2^{10} \bmod 11 = 1$ , 11 is pseudo(-Fermat)-prime base 2.
- $3^{10} \bmod 11 = 1$ , 11 is pseudo(-Fermat)-prime base 3.

Calculate  $\Phi(19)$ ,  $\Phi(15)$ ,  $\Phi(8)$

- $\Phi(19) = 19 - 1 = 18$
- $\Phi(15) = 5 * 3 = (5-1)(3-1) = 8$
- $\Phi(8) = \Phi(2^3) = 2^2(2-1) = 4$

Calculate  $5^{13} \bmod 71$  using the fast exponentiation algorithm.

**a=5, n=71**

**e=13= (1101)<sub>2</sub> m=4**

|         |   |    |   |    |
|---------|---|----|---|----|
| i       | - | 2  | 1 | 0  |
| ei      | 1 | 1  | 0 | 1  |
| r       | 5 | 25 | 5 | 25 |
| $R=r*a$ |   | 54 |   | 54 |

### Exercise No. 2: (RSA encryption)

Let  $p = 7$  and  $q = 19$

1. Describe the key generation scheme, encryption scheme, and decryption scheme.

See the course

2. Show that  $D(E(m)) = m$ .

$$D(E(m)) = D(me \bmod n) = (me)d \bmod n = med \bmod n$$

$$\text{knowing that } ed = 1 \bmod \Phi(n) = k\Phi(n) + 1$$

$$\text{then } D(E(m)) = mk^{\Phi(n)+1} \bmod n = m$$

3. Calculate  $N$  and  $\Phi(n)$ .

$$N = pq = 133 \text{ and } \Phi(n) = (p-1)(q-1) = 108$$

4. We propose  $e = 5$ . Calculate the private key  $d$ .

$$ed = 1 \bmod \Phi(n) \quad d = e^{-1} \bmod \Phi(n)$$

$$d = 5^{-1} \bmod 108 = 65$$

5. Encrypt the plaintext  $m = 6$ .

$$C = m^e \bmod n = 6^5 \bmod 133 = 62$$

6. Decrypt the ciphertext  $c = 62$ .

$$M = c^d \bmod n = 62^{65} \bmod 133 = 6$$

## Exercise No. 2: (Diffie-Hellman Protocol)

1. What is the purpose of the Diffie-Hellman protocol?

Key exchange

2. Determine the Diffie-Hellman session key if Alice communicates the numbers  $g = 3$  and  $p = 23$  to Bob, given that Alice selects the random number  $a = 5$  and Bob selects the number  $b = 7$ .

The session key calculated in the Diffie-Hellman protocol is  $K = g^{xy} \bmod p$

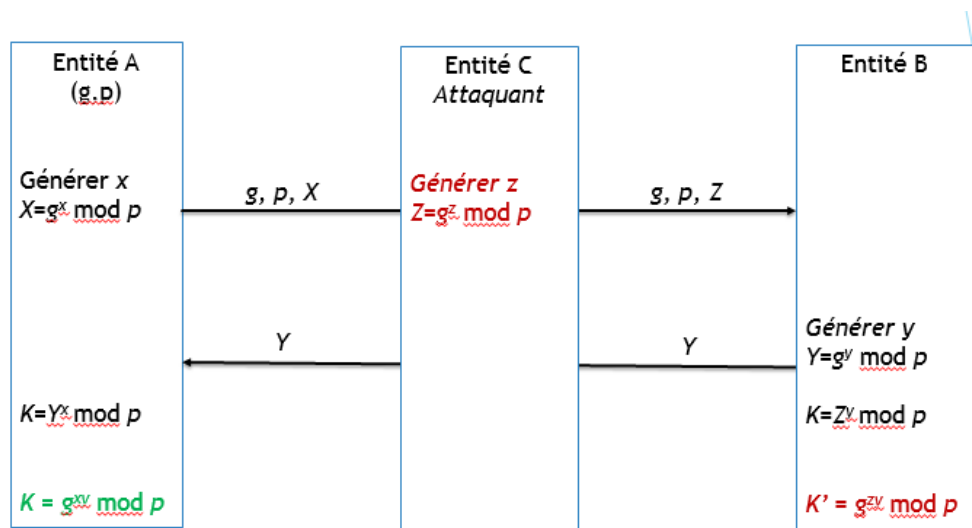
It's necessary to calculate X and Y.

$$K = 3^{5 \cdot 7} \bmod 23 = 9$$

3. Explain the weaknesses of the Diffie-Hellman protocol.

The Diffie-Hellman protocol is vulnerable to man-in-the-middle attacks.

4. Propose a MITM type attack scenario.



## Exercise No. 4: (Hash Functions)

- What properties must hash functions check?

Pre-image resistance, Second pre-image resistance, Collision resistance

- Give examples of applications of hash functions.

- Password protection,
- Pseudo-random number generator,
- Message authentication code (MAC),
- Deriving session keys.
- Blockchain.
- Compress messages during digital signature generation and verification.

- What is the difference between MDC and HMAC type functions?

| MDC | HMAC |
|-----|------|
|-----|------|

|                                                                                                                                                                                                                                       |                                                                                                                                                                                                                                                                                         |
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| <ul style="list-style-type: none"> <li>▶ A hash function <math>H</math> that can be computed without knowledge of a secret.</li> <li>▶ Ensures integrity.</li> <li>▶ The function is defined as follows: <math>H(m)</math></li> </ul> | <ul style="list-style-type: none"> <li>▶ Ensures integrity and authentication</li> <li>▶ is a type of message authentication code (MAC), calculated using a hash function in combination with a secret key.</li> <li>▶ HMAC security is dependent on the hash function used.</li> </ul> |
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- Which of these hash functions are secure: MD-5, SHA-3, SHA-1, SHA-512?

SHA-3, SHA-512.

- Why is a hash function a better way to verify integrity than a checksum such as the Internet checksum?

The properties of the hash function are not applied for Internet checksum.