

## Solutions for Tutorial Session N°5 : Deadlock

**Objective:** To understand the concept of deadlock in operating systems, identify the conditions under which it occurs, and explore the main techniques used for deadlock prevention, avoidance, detection, and recovery.

### Exercise 1

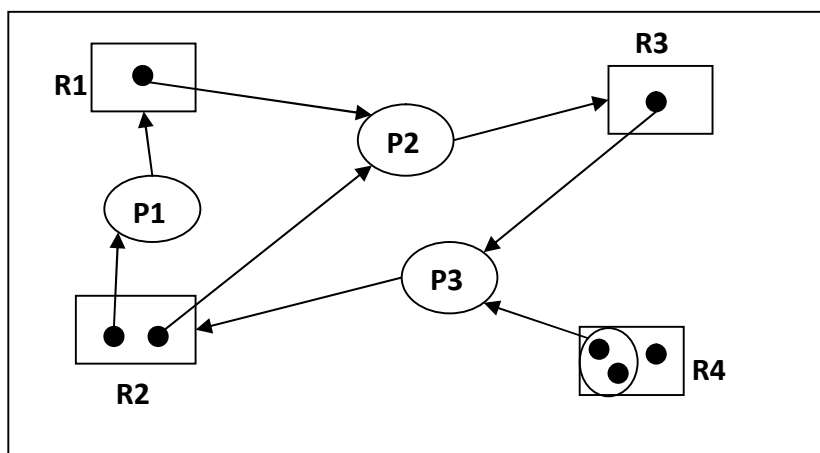
Consider a system with 3 processes P1, P2, P3, and 4 types of resources R1, R2, R3, R4, with a single instance for R1 and R3, 2 instances for R2, and 3 instances for R4. Consider the following resource allocation:

- P1 holds R2 and requests R1;
- P2 holds R1, R2 and requests R3;
- P3 holds R3 and 2 instances of R4, and requests R2;

Construct the resource allocation graph. Is there a deadlock? If so, which processes are involved?

### SOLUTION

1) The resource allocation graph



2) Deadlocks?

- Cycle 1: P2, R3, P3, R2, P2 ==> deadlock between P2 and P3
- Cycle 2: P1, R1, P2, R3, P3, R2, P1 ==> deadlock between P1, P2 and P3

## Exercise 2

Consider a system with 5 processes (P0, P1, P2, P3, P4) and 3 resource types (R0, R1, R2). The state of the system is:

| MAX |    |    |    | ALLOCATION |    |    |    | AVAILABLE |    |    |
|-----|----|----|----|------------|----|----|----|-----------|----|----|
|     | R0 | R1 | R2 |            | R0 | R1 | R2 | R0        | R1 | R2 |
| P0  | 7  | 5  | 3  | P0         | 0  | 1  | 0  | 3         | 3  | 2  |
| P1  | 3  | 2  | 2  | P1         | 2  | 0  | 0  |           |    |    |
| P2  | 9  | 0  | 2  | P2         | 3  | 0  | 2  |           |    |    |
| P3  | 2  | 2  | 2  | P3         | 2  | 1  | 1  |           |    |    |
| P4  | 4  | 3  | 3  | P4         | 0  | 0  | 2  |           |    |    |

- How many instances are there for each resource in this system?
- Calculate the **NEED** matrix.
- Determine if the system is in a safe state using the **Banker's algorithm**.
- Assuming the system receives the following requests sequentially, determine at each moment whether the request can be granted or not (**Banker's algorithm**):
  - At time t1, P1 makes the following request: (1, 0, 2).
  - At time t2, P4 makes the following request: (3, 3, 0).
  - At time t3, P0 makes the following request: (0, 2, 0).

## SOLUTION

1)

| Resource | Number of instances (AVAILABLE + ALLOCATION) |
|----------|----------------------------------------------|
| R0       | 3+2+3+2 = 10                                 |
| R1       | 3+1+1= 5                                     |
| R2       | 2+2+1+2= 7                                   |

2) NEED = MAX – ALLOCATION:

|    | R0 | R1 | R2 |
|----|----|----|----|
| P0 | 7  | 4  | 3  |
| P1 | 1  | 2  | 2  |
| P2 | 6  | 0  | 0  |
| P3 | 0  | 1  | 1  |
| P4 | 4  | 3  | 1  |

3) Banker's Safety algorithm:

| Work   |    |    |    | Finish |    |    |    |    |
|--------|----|----|----|--------|----|----|----|----|
| Steps  | R0 | R1 | R2 | P0     | P1 | P2 | P3 | P4 |
| Step 0 | 3  | 3  | 2  | F      | F  | F  | F  | F  |
| Step 1 | 5  | 3  | 2  | F      | T  | F  | F  | F  |
| Step 2 | 7  | 4  | 3  | F      | T  | F  | T  | F  |
| Step 3 | 7  | 4  | 5  | F      | T  | F  | T  | T  |
| Step 4 | 7  | 5  | 5  | T      | T  | F  | T  | T  |
| Step 5 | 10 | 5  | 7  | T      | T  | T  | T  | T  |

The system is in a safe state: the sequence P1, P3, P4, P0, P2 is safe.

4)

**P1 makes the following request: (1, 0, 2)**

$(1, 0, 2) \leq \text{NEED}[1]$  and  $(1, 0, 2) \leq \text{AVAILABLE}$

We assume that the request is granted and update the data:

- $\text{Available} = \text{Available} - \text{Request}[i]$
- $\text{Allocation}[i] = \text{Allocation}[i] + \text{Request}[i]$
- $\text{Need}[i] = \text{Need}[i] - \text{Request}[i]$

| NEED      |          |          |          | ALLOCATION |          |          |          | AVAILABLE |    |    |
|-----------|----------|----------|----------|------------|----------|----------|----------|-----------|----|----|
|           | R0       | R1       | R2       |            | R0       | R1       | R2       | R0        | R1 | R2 |
| P0        | 7        | 4        | 3        | P0         | 0        | 1        | 0        | 2         | 3  | 0  |
| <b>P1</b> | <b>0</b> | <b>2</b> | <b>0</b> | <b>P1</b>  | <b>3</b> | <b>0</b> | <b>2</b> |           |    |    |
| P2        | 6        | 0        | 0        | P2         | 3        | 0        | 2        |           |    |    |
| P3        | 0        | 1        | 1        | P3         | 2        | 1        | 1        |           |    |    |
| P4        | 4        | 3        | 1        | P4         | 0        | 0        | 2        |           |    |    |

Afterwards, we apply the **safety algorithm**:

| Work   |    |    |    | Finish |    |    |    |    |
|--------|----|----|----|--------|----|----|----|----|
| Steps  | R0 | R1 | R2 | P0     | P1 | P2 | P3 | P4 |
| Step 0 | 2  | 3  | 0  | F      | F  | F  | F  | F  |
| Step 1 | 5  | 3  | 2  | F      | T  | F  | F  | F  |
| Step 2 | 7  | 4  | 3  | F      | T  | F  | T  | F  |
| Step 3 | 7  | 4  | 5  | F      | T  | F  | T  | T  |
| Step 4 | 7  | 5  | 5  | T      | T  | F  | T  | T  |
| Step 5 | 10 | 5  | 7  | T      | T  | T  | T  | T  |

- We find that the sequence P1, P3, P4, P0, P2 is safe, so P1's request can be granted.
- The OS confirms the changes made to the **ALLOCATION** and **NEED** matrices, and the **AVAILABLE** vector.

**P4 makes the following request: (3, 3, 0)**

$(3, 3, 0) \leq \text{NEED}[4]$

but  $(3, 3, 0) > \text{AVAILABLE}$

Therefore, this request cannot be granted, and P4 remains waiting (blocked).

**P0 makes the following request: (0, 2, 0)**

$(0, 2, 0) \leq \text{NEED}[0]$  and  $(0, 2, 0) \leq \text{AVAILABLE}$

We assume that the request is granted and update the data:

- **Available = Available – Request[i]**
- **Allocation[i] = Allocation[i] + Request[i]**
- **Need[i] = Need[i] – Request[i]**

| NEED      |          |          |          | ALLOCATION |          |          |          | AVAILABLE |          |          |
|-----------|----------|----------|----------|------------|----------|----------|----------|-----------|----------|----------|
|           | R0       | R1       | R2       |            | R0       | R1       | R2       | R0        | R1       | R2       |
| <b>P0</b> | <b>7</b> | <b>2</b> | <b>3</b> | <b>P0</b>  | <b>0</b> | <b>3</b> | <b>0</b> | <b>2</b>  | <b>1</b> | <b>0</b> |
| P1        | 0        | 2        | 0        | P1         | 3        | 0        | 2        |           |          |          |
| P2        | 6        | 0        | 0        | P2         | 3        | 0        | 2        |           |          |          |
| P3        | 0        | 1        | 1        | P3         | 2        | 1        | 1        |           |          |          |
| P4        | 4        | 3        | 1        | P4         | 0        | 0        | 2        |           |          |          |

Now, we apply the **safety algorithm**:

| Work   |    |    |    | Finish   |          |          |          |          |
|--------|----|----|----|----------|----------|----------|----------|----------|
| Steps  | R0 | R1 | R2 | P0       | P1       | P2       | P3       | P4       |
| Step 0 | 2  | 1  | 0  | <b>F</b> | <b>F</b> | <b>F</b> | <b>F</b> | <b>F</b> |

- There is no **i** such that **Finish[i] == false** and **Need[i] ≤ Work**, so the system is not in a safe state; all 5 processes are in deadlock. Therefore, the request cannot be granted.
- The OS keeps (restores) the previous values of the **ALLOCATION** and **NEED** matrices, and the **AVAILABLE** vector.

### Exercise 3

Consider the following systems. Use the **deadlock detection algorithm** to determine whether the processes in each system are in deadlock or not:

#### 1) System A :

| ALLOCATION |    |    |    |    | REQUEST |    |    |    |    | AVAILABLE |    |    |    |
|------------|----|----|----|----|---------|----|----|----|----|-----------|----|----|----|
|            | R0 | R1 | R2 | R3 |         | R0 | R1 | R2 | R3 | R0        | R1 | R2 | R4 |
| P0         | 1  | 0  | 1  | 0  | P0      | 2  | 3  | 0  | 1  | 5         | 2  | 3  | 1  |
| P1         | 2  | 0  | 0  | 1  | P1      | 2  | 0  | 1  | 0  |           |    |    |    |
| P2         | 0  | 1  | 2  | 0  | P2      | 2  | 1  | 4  | 0  |           |    |    |    |

#### 2) System B :

| ALLOCATION |    |    |    | REQUEST |    |    |    | AVAILABLE |    |    |
|------------|----|----|----|---------|----|----|----|-----------|----|----|
|            | R0 | R1 | R2 |         | R0 | R1 | R2 | R0        | R1 | R2 |
| P0         | 0  | 1  | 0  | P0      | 0  | 0  | 0  | 0         | 0  | 0  |
| P1         | 2  | 0  | 0  | P1      | 2  | 0  | 2  |           |    |    |
| P2         | 3  | 0  | 2  | P2      | 0  | 0  | 0  |           |    |    |
| P3         | 2  | 1  | 1  | P3      | 1  | 0  | 0  |           |    |    |
| P4         | 0  | 0  | 2  | P4      | 0  | 0  | 2  |           |    |    |

### SOLUTION

#### 1) System A :

| ALLOCATION |    |    |    |    | REQUEST |    |    |    |    | AVAILABLE |    |    |    |
|------------|----|----|----|----|---------|----|----|----|----|-----------|----|----|----|
|            | R0 | R1 | R2 | R3 |         | R0 | R1 | R2 | R3 | R0        | R1 | R2 | R4 |
| P0         | 1  | 0  | 1  | 0  | P0      | 2  | 3  | 0  | 1  | 5         | 2  | 3  | 1  |
| P1         | 2  | 0  | 0  | 1  | P1      | 2  | 0  | 1  | 0  |           |    |    |    |
| P2         | 0  | 1  | 2  | 0  | P2      | 2  | 1  | 4  | 0  |           |    |    |    |

The execution of the **deadlock detection algorithm** will reveal the following contents:

For  $i = 0..n-1$ , if  $\text{Allocation}[i] \neq 0$ , then  $\text{Finish}[i] = \text{false}$ ; otherwise  $\text{Finish}[i] = \text{true}$   
**→ so here Finish = (F, F, F)**

**Work**

| Steps  | R0 | R1 | R2 | R3 |
|--------|----|----|----|----|
| Step 0 | 5  | 2  | 3  | 1  |
| Step 1 | 7  | 2  | 3  | 2  |

**Finish**

| P0 | P1 | P2 |
|----|----|----|
| F  | F  | F  |
| F  | T  | F  |

The algorithm execution ends with the **Finish** vector containing two false values: **P0 and P2 are in deadlock.**

**Note: The OS must apply one of the recovery techniques to resolve this deadlock situation.**

## 2) System B :

**ALLOCATION**

|    | R0 | R1 | R2 |
|----|----|----|----|
| P0 | 0  | 1  | 0  |
| P1 | 2  | 0  | 0  |
| P2 | 3  | 0  | 2  |
| P3 | 2  | 1  | 1  |
| P4 | 0  | 0  | 2  |

**REQUETE**

|    | R0 | R1 | R2 |
|----|----|----|----|
| P0 | 0  | 0  | 0  |
| P1 | 2  | 0  | 2  |
| P2 | 0  | 0  | 0  |
| P3 | 1  | 0  | 0  |
| P4 | 0  | 0  | 2  |

**DISPONIBLE**

| R0 | R1 | R2 |
|----|----|----|
| 0  | 0  | 0  |

The execution of the algorithm gives us the following steps:

**Work**

| Steps  | R0 | R1 | R2 |
|--------|----|----|----|
| Step 0 | 0  | 0  | 0  |
| Step 1 | 0  | 1  | 0  |
| Step 2 | 3  | 1  | 2  |
| Step 3 | 5  | 2  | 3  |
| Step 4 | 5  | 2  | 5  |
| Step 5 | 7  | 2  | 5  |

**Finish**

| P0 | P1 | P2 | P3 | P4 |
|----|----|----|----|----|
| F  | F  | F  | F  | F  |
| T  | F  | F  | F  | F  |
| T  | F  | T  | F  | F  |
| T  | F  | T  | T  | F  |
| T  | F  | T  | T  | T  |
| T  | T  | T  | T  | T  |

The sequence P0, P2, P3, P4, P1 will set **Finish[i]** to true for all i, so the system is not in deadlock.