

Faculty of Mathematics and informatics
Computer science department
Level: L2
Course: Theory of computation
A/Y: 2024/2025

5th Practical Series

Push Down Automata

Let $A = \{a, b\}$ be an alphabet, and Let $L = \{a^n b^n, n \in \mathbb{N}\}$ be a language on A

As we have proved, in our course this language is not regular, in other words, we cannot use the finite automata to recognize it,

This language is a context-free language, because it exists a context free grammar that generates it: $G = (N, T, S, P)$, $N = \{S\}$, $T = \{a, b\}$, $P = \{S \rightarrow aSb \mid \varepsilon\}$, an alternative solution is used through the Push Down Automata (PDA), which is a 7-tuples:

$$M = (Q, \Sigma, S, \delta, q_0, Z_0, F)$$

Q : finite set of states.

Σ : input alphabet

S : stack symbols

δ : transition function $Q \times (\Sigma \cup \{\varepsilon\}) \times S \rightarrow Q \times S^*$

$q_0 \in Q$: initial state

$z_0 \in S$: initial stack top symbol

$F \subseteq Q$: set of accepting states.

- Build a Push Down Automaton that recognizes $L(G)$
- Show the acceptance sequence on the few given words (examples) by the PDA.
 - By final state, then by empty stack acceptability.